

A 0.3-V, 37.5-nW 1.5~6.5-pF-Input-Range Supply Voltage Tolerant Capacitive Sensor Readout

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Abstract—A fully-digital capacitive sensor readout circuit based on capacitance controlled oscillators is presented. A two-step quantization scheme using SAR for coarse conversion and $\Delta\Sigma$ for fine conversion is introduced to extend the sensor input range while preserving the sensing accuracy. Systematic error analysis and optimization for the finite switch on-resistance and buffer input dependent delay are also outlined. Power supply insensitivity is ensured by the use of a pseudo-differential architecture and a ratiometric readout scheme. The complete sensor readout is implemented in a standard 0.18 μm CMOS process. Simulation results show that the sensor readout circuit can achieve a wide input range from 1.5 to 6.5pF and a worst case power supply rejection ratio of 0.65% from 0.3V to 0.6V. For the $\Delta\Sigma$ conversion, a resolution of 7.4b at a conversion frequency of 318 Hz with an input capacitance of 4pF and a 0.3V supply is achieved. An average power is 37.5nW at 0.3V with a 4pF input capacitance, corresponding to a Figure-of-Merit (FoM) of 350fJ/conv-step.

I. INTRODUCTION

The limited energy capacity has always been one of the major bottlenecks in wireless sensing systems such as portable biomedical devices and wireless sensor networks [1]. To solve this problem, systems equipped with energy scavengers and ultra-low power high efficiency electronics are generally practiced to achieve system autonomous and extend system lifetime. Despite the advantages of energy harvesting systems, the environmental energy typically does not spread homogeneously. The temporal fluctuation induced supply noise and the low voltage generated (typically between 0.3V and 0.6V depends on different illumination conditions) present major challenges for designing a high accuracy sensor readout circuit with ultra-low power consumption using such energy source. This work focuses on the design of a capacitive sensor readout that can be powered directly by solar energy harvesters.

In [2], a ring-oscillator-based sensor readout circuit directly supplied by integrated photodiodes is demonstrated. Due to the strong dependency between the supply voltage and the oscillation frequency, large readout error exists under different illumination conditions, jeopardizing the system

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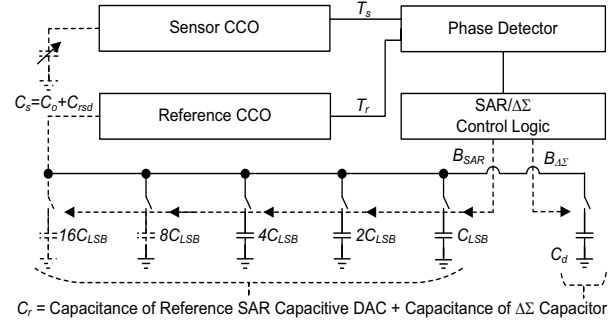


Fig. 1. The proposed two-step capacitive sensor readout.

robustness. This supply variation issue is resolved in [3] by inserting a linear regulator to provide a stable supply voltage to the sensor readout circuit. However, this inevitably induces extra energy loss, penalizing the system energy efficiency. In [4], a high sensor readout accuracy is achieved by improving the supply insensitivity using a force-balanced Wheatstone bridge and differential Maneatis-cells. However, a relatively high minimum supply voltage of 0.85V is necessary and extra DC-DC conversion stages may be needed if it is powered by solar energy harvesters. In [5], a fully-digital capacitive sensor interface that can operate at a supply voltage down to 0.3V is presented. An estimated power supply rejection ratio (PSRR) of 1.2% is achieved by using a pseudo-differential architecture and a ratiometric readout scheme. However, this topology is sensitive to the variation in the sensor offset capacitance. It also has a narrow input sensing range ($\sim 300\text{fF}$) due to the distortion and mismatch introduced in the readout paths, limiting its potential for application area.

This work presents a fully-digital two-step SAR/ $\Delta\Sigma$ capacitive sensor readout with a wide input-range of 1.5~6.5pF. It can operate under a supply voltage from 0.3 to 0.6V, and can be directly powered by solar energy harvesters without extra DC-DC conversion. By using two capacitance-controlled-oscillators (CCOs) in pseudo-differential configuration and a ratiometric readout scheme, a PSRR of 0.65% within the targeted supply range is achieved. This paper is organized as follows. Section II outlines the proposed two-step wide-range sensor readout circuit architecture with a systemic error source analysis. Section III provides the simulation results of the proposed readout circuit using a standard 0.18 μm CMOS technology. The conclusion is given in section IV.

II. SYSTEM OVERVIEW

A. Two-Step Capacitive Sensor Readout Architecture

Fig. 1 shows the block diagram of the proposed two-step capacitive sensor readout, which is composed of two

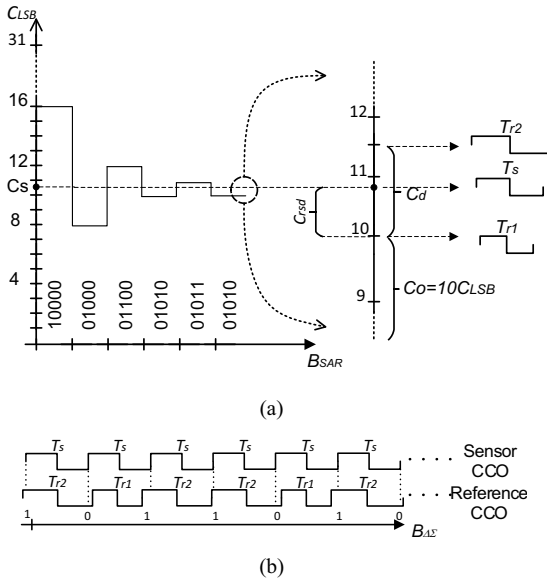


Fig. 2. A complete conversion cycle of the proposed capacitive sensor readout: (a) Coarse SAR conversion stage; (b) Fine conversion stage.

CCOs, a phase detector, a SAR/ $\Delta\Sigma$ control logic, a SAR capacitor array and a $\Delta\Sigma$ capacitor C_d . The coarse detection and fine detection are performed by the SAR capacitor array and the $\Delta\Sigma$ capacitor, respectively, with the SAR stage to cancel the sensor offset capacitance C_o and the $\Delta\Sigma$ stage to convert the sensor residue capacitance $C_{r,sd}$. Fig. 2 shows a complete conversion cycle of the proposed capacitive sensor readout. At the beginning of the coarse conversion, the control logic first configures the converter into SAR mode (course conversion stage). During this period, the two CCOs perform capacitance-to-time conversion and generate two time signals T_s and T_r corresponding to the sensor capacitance C_s and the reference capacitance C_r , respectively. Their phase difference is then determined and digitized by the phase detector. The generated digital output is then fed back to the SAR capacitor array to perform successive approximation. At the end of the course conversion, a 5-b digital output B_{SAR} results and is utilized in the following fine conversion stage. The control logic block controls B_{SAR} so that T_r should be strictly smaller than T_s to ensure proper $\Delta\Sigma$ conversion, and configures the sensor readout into $\Delta\Sigma$ mode to maximize hardware reuse. During the fine conversion, C_d is utilized for signal conversion and T_r switches to either T_{r1} or T_{r2} depending on the output bit in each cycle. The two CCOs act as time integrators to perform first-order noise-shaping. The output bitstream $B_{\Delta\Sigma}$ can then be combined with B_{SAR} to generate the final digital output. This two-step conversion takes advantage of the fast SAR conversion and the high resolution $\Delta\Sigma$ readout to achieve improved energy efficiency. The introduction of the SAR stage can also resolve the intrinsic limited sensing range as in a standalone $\Delta\Sigma$ implementation, and will be discussed further in section II.B.2.

B. Design Considerations

Fig. 3 shows the detailed implementation of the capacitive sensor readout. Two inverter-based CCOs are constructed using a signal conversion stage followed by buffers. The capacitive sensor C_s and the capacitive array are inserted within the corresponding signal conversion stage. The outputs

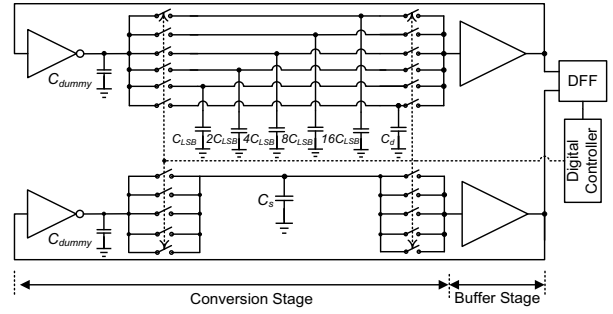


Fig. 3. The detailed implementation of the capacitive sensor readout.

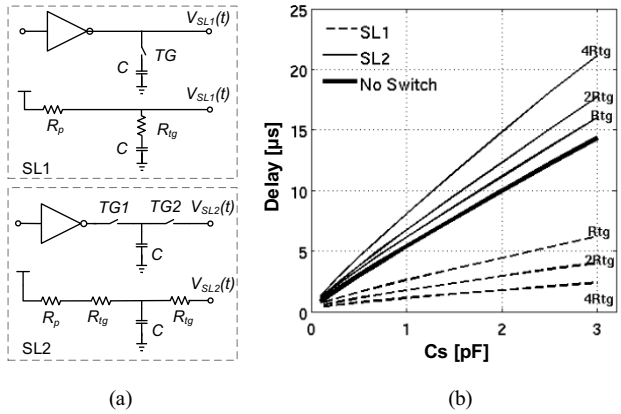


Fig. 4. (a) Switch location one (SL1) and switch location two (SL2) using transmission gate with charging phase equivalent model; (b) Delay vs. C_s at different switch locations with changing switch widths.

from the CCOs are compared using a D-Flipflop (DFF) and the result is forwarded to the control logic for proper conversion operations. Even though the circuit can operate at ultra-low voltage operation for improved energy performance, this also limits the use of cascading stages which can significantly jeopardize the PSRR of the capacitive sensor readout. The non-ideal effect of switch charge error have investigated in [8] and have solved by a new switching and calibration schemes. However according to our circuit the effect of increased switch impedance is a mainly limitation. Another detrimental effect on the sensor readout performance is the non-ideal buffer delay as a result of the low-supply voltage. This section investigates each of these non-ideal effects to achieve optimized sensor readout performance.

1) Switch Arrangements

Due to the finite on- and off-resistance of CMOS switches, the implementation and arrangement of the switches is imperative to improve the sensor readout performance. To reduce the input dependent switch resistance effect, all the switches are implemented using transmission gates. Fig. 4(a) shows two different switch arrangements SL1 and SL2 for capacitor selection, where the switches are arranged in two different configurations. With R_p and R_{tg} denote the average on resistance of a PMOS and transmission gate in the charging phase, respectively. Without loss of generality, we only consider the charging phase in the following analysis. During the charging period, the two voltages at the output nodes as shown in Fig. 4(a) are given by

$$V_{SL1}(t) = V_{DD} \left(1 - \frac{R_p}{R_p + R_{tg}} e^{-t/\tau_{SL1}} \right) \quad (1)$$

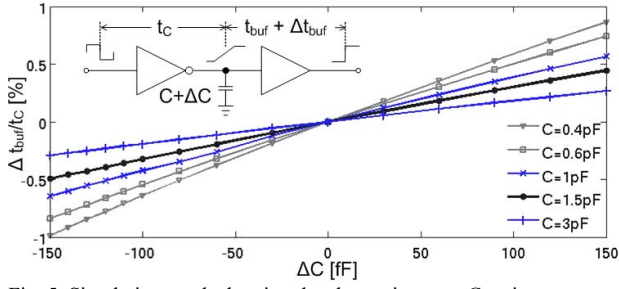


Fig. 5. Simulation result showing the change in t_{buf} as C varies.

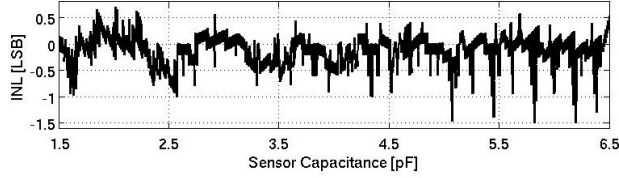


Fig. 6. Simulated INL for the complete sensor readout circuit.

$$V_{SL2}(t) = V_{DD}(1 - e^{-t/\tau_{SL2}}) \quad (2)$$

where τ_{SL1} and τ_{SL2} denote the corresponding charging time constant with

$$\tau_{SL1} = \tau_{SL2} = \tau_{cha} = (R_p + R_{tg})C \quad (3)$$

Notice that the effect of $TG2$ in Fig. 4(a). $SL2$ is negligible as it is connected to a buffer with high input impedance. Assuming the trip point of next stage inverter is $0.5V_{DD}$, the delays in the charging phase can be expressed as

$$t_{SL1} = \tau_{cha} \ln \frac{2R_p}{R_p + R_{tg}} \quad (4)$$

$$t_{SL2} = \tau_{cha} \ln 2 \quad (5)$$

It can be observed that $t_{SL1} < t_{SL2}$ for all realistic values of R_p and R_{tg} , which denote the capacitance to time gain of $SL2$ is larger than $SL1$, with the switch arrangement in Fig. 4(a). $SL2$ should be chosen to achieve increased time domain signal power under the same power budget. Fig. 4. (b) shows the simulation result of the propagation delay without switch, with $SL1$ and with $SL2$, respectively. It is shown that an increased signal delay can be achieved by using the $SL2$ and vice versa. It should be noted that the two switch arrangements deviate from the no switch case with decreasing R_{tg} .

2) Buffer Stage Propagation Delay

Except from the signal conversion stage, the buffer stage which are implemented using even number of inverters, also generates finite delay that affect the CCO oscillation frequency (f_{CCO}), which is defined as

$$\frac{1}{f_{CCO}} = t_c + t_{buf} \quad (6)$$

where t_c and t_{buf} denote the total delay in both charging and discharging phases for the signal conversion stage and the buffer stage, respectively. Ideally, t_{buf} should be the intrinsic delay which is signal independent. But as the input rise/fall time of the buffer stage deviates from the ideal step input, t_{buf} becomes input signal dependent that can increase the signal distortion at the converter output, and affects both the SAR

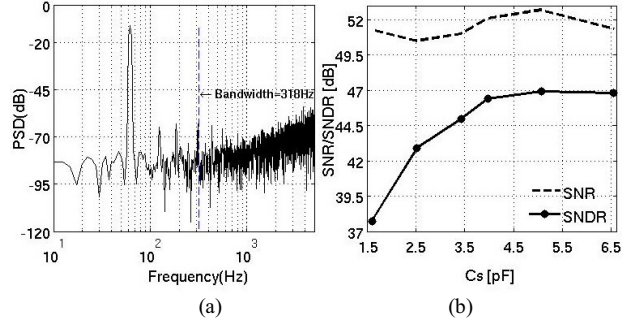


Fig. 7. (a) Simulated output spectrum with $f_{in}=62.1\text{Hz}$, $C_s=4\text{pF}$ and an amplitude of 100fF ; (b) SNR/SNDR versus different C_s .

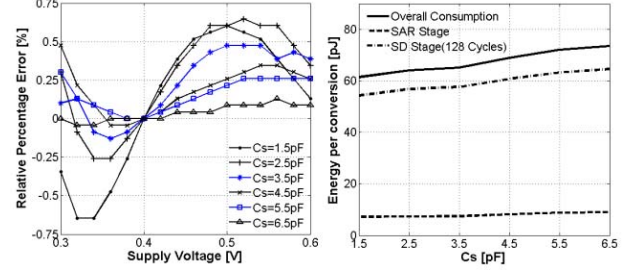


Fig. 8. (a) Relative percentage error versus supply voltage with different C_s ; (b) Energy per conversion of the SAR stage, $\Delta\Sigma$ stage and the entire sensor readout.

and $\Delta\Sigma$ conversion. Fig. 5 illustrates the simulation result of the change in t_{buf} as C varies using the schematic as shown, and the dependency becomes significant as C reduces. To solve this problem, C_{dummy} with a value of 1.5pF is added in parallel to C_s and C_r as shown in Fig. 3. Using Fig. 5, to achieve an error of 0.5% with $\Delta C = \pm 150\text{fF}$, $C_{dummy} + C_{s,min}$ should be set to 3pF , and the corresponding C_{LSB} and C_d are set to 200fF and 300fF , respectively.

3) Power Supply Rejection

During the coarse detection, C_r will approach C_o and the residue error C_{rsd} is within 200fF . In order to avoid missing codes, C_d is set to 300fF to introduce redundancy during the $\Delta\Sigma$ operation. With B_1 denoting the ratio between the number of ones and the total number of bits in the $\Delta\Sigma$ output bit stream, the following relationship between the oscillation frequencies of the sensor CCO and reference CCO can be obtained

$$\frac{1 - B_1}{f_{CCO}} \Big|_{C_r=C_o} + \frac{B_1}{f_{CCO}} \Big|_{C_r=C_o+C_d} = \frac{1}{f_{CCO}} \Big|_{C_s} \quad (7)$$

With a C_{dummy} of 1.5pF and a worst case difference between C_r and C_s of 300fF , the result in $\Delta t_{buf}/t_c$ is within 0.5% (as illustrated in section II.B2), meaning that $t_{buf}|_{C_r=C_o} \approx t_{buf}|_{C_r=C_o+C_d} \approx t_{buf}|_{C_s}$ in the covered $\Delta\Sigma$ sensing range. By using (6) and (7),

$$(1 - B_1) \times t_{c=C_o} + B_1 \times t_{c=C_o+C_d} = t_{c=C_o+C_{rsd}} \quad (8)$$

The conversion stage delay of charging phase is given by (5). For any capacitor C , the corresponding time constant during the discharging phase is equal to $(R_n + R_{tg})C$, and the total delay t_c can be expressed as

TABLE I. PERFORMANCE COMPARISON

	[4]	[5]	[6]	[7]	This Work
Topology	$\Delta\Sigma$	$\Delta\Sigma$	SAR	PWM	SAR/ $\Delta\Sigma$
Capacitive(C)/Resistive(R)	R	C	C	C	C
Sensor Range	2 k Ω	5.7~6 pF	50~53 pF	0.5~0.7 pF	1.5~6.5 pF
Supply Voltage (V)	1	0.3	1.4	3	0.3~0.6
ENOB	8.9b	6.1b	6.8b	8b	7.4b ⁽¹⁾
Power (μ W)	124.5	0.27	236.6	84	0.0375 ⁽¹⁾
Conversion Freq.(Hz)	10M	1k	0.26M	30k	318 ⁽¹⁾
PSRR@DC	0.7%	1.2% ⁽²⁾	-	-	0.65% ⁽³⁾
FoM (pJ/conv-step)	13.03	3.9	7.9	10	0.35 ⁽¹⁾

⁽¹⁾ Simulation result at 300mV supply with $C_s = 4$ pF ($\Delta\Sigma$ only).

⁽²⁾ Estimated from the corresponding paper.

⁽³⁾ Worst case over the entire sensing range.

$$t_c = (R_p + R_n + 2R_{tg})C \ln 2 \quad (9).$$

As the equivalent resistance in (9) is sensitive to the supply voltage variation, t_c is also prone to supply noise, resulting in a supply sensitive CCO output frequency. With a ratiometric readout scheme, the supply sensitive term can be effectively cancelled. By substituting (9) into (8),

$$C_{rsd} = B_1 \times C_d \quad (10)$$

Theoretically, the power supply noise should be completely cancelled. However, the residues between different t_{buf} and the mismatch in R_p , R_n and R_{tg} between the two CCOs can lead to finite PSRR. With the use of the coarse SAR conversion, the two CCOs can be better matched, improving the PSRR of the capacitive sensor readout. The use of a small C_d can also improve the linearity of the $\Delta\Sigma$ conversion, and the resolution is mainly limited by the phase noise of the CCOs [5].

III. SIMULATION RESULTS

The complete capacitive sensor readout circuit is implemented using a 0.18 μ m standard CMOS process, with C_s ranging from 1.5pF to 6.5pF using a supply voltage of 0.3V. An Over-Sampling-Ratio (OSR) of 128 is used during the fine $\Delta\Sigma$ conversion. Fig. 6 shows the simulated INL of the two-step capacitive sensor readout. It can be observed that an INL of +0.5/-1.5 LSB can be achieved in the entire input range, and is limited by the linearity and the capacitance mismatch of the two CCOs. Fig. 7(a) shows the simulated output spectrum with a mean input capacitance of 4pF and a peak-to-peak variation of 100fF at 62.1Hz. The sampling frequency and entire conversion frequency for the complete sensor readout are 81.4 kHz and 291 Hz, respectively. The calculated SNDR is 46.4dB, corresponding to a resolution of 7.4b. Fig. 7(b) shows the SNR/SNDR plot with the same settings using a mean input capacitance from 1.5pF to 6.5pF. It can be seen that the worst case occurs at minimum C_s as expected.

Fig. 8(a) shows the relative percentage error with the supply voltage varying from 0.3 to 0.6V. The relative error reduces as C_s increases also, and the error is within 0.65%. Fig. 8(b) shows the energy per conversion of the sensor readout circuit. The required energy increases as C_s increases as expected. The SAR part only consumes less than 10pJ per conversion and is therefore negligible. For the $\Delta\Sigma$ stage, the sampling frequency ranges from 88kHz to 73kHz, consuming an average power of 37.5nW. By using the Figure-of-Merit (FoM) as

$$FoM = \frac{P}{2^{ENOB} \times 2 \times Bandwidth}, \quad (10)$$

the proposed capacitive sensor readout circuit achieves a FoM of 349.8fJ/conv-step. Table I shows the performance comparisons with recent sensor readout circuit publications.

IV. CONCLUSION

A fully-digital capacitive sensor readout circuit with wide input-range of 1.5~6.5pF that can operate with a supply voltage of as low as 0.3V in 0.18 μ m CMOS is presented. Non-idealities including the switch resistance and buffer stage propagation delay and their effect on the sensor readout performance are systematically analyzed. Simulation results show by using time-based pseudo-differential CCOs and ratiometric readout scheme, a PSRR of 0.65% from 0.3V to 0.6V is achieved. The sensor readout circuit consumes an average power of 37.5nW at 0.3V supply, and the achieved FoM for the $\Delta\Sigma$ conversion stage is 350fJ/conv.

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